Serial interval in determining the estimation of reproduction number of the novel coronavirus disease (COVID-19) during the early outbreak

Shi Zhao MPhil\textsuperscript{1,2,*}, Peihua Cao PhD\textsuperscript{3}, Daozhou Gao PhD\textsuperscript{4}, Zian Zhuang Bsc\textsuperscript{5}, Yongli Cai PhD\textsuperscript{6}, Jinjun Ran MPhil\textsuperscript{7}, Marc KC Chong PhD\textsuperscript{1,2}, Kai Wang PhD\textsuperscript{8}, Yijun Lou PhD\textsuperscript{5}, Weiming Wang PhD\textsuperscript{6,*}, Lin Yang PhD\textsuperscript{9}, Daihai He PhD\textsuperscript{5,*}, and Maggie H Wang PhD\textsuperscript{1,2}

1 JC School of Public Health and Primary Care, Chinese University of Hong Kong, Hong Kong, China
2 Shenzhen Research Institute of Chinese University of Hong Kong, Shenzhen, China
3 Clinical Research Centre, Zhujiang Hospital, Southern Medical University, Guangzhou, Guangdong, China
4 Department of Mathematics, Shanghai Normal University, Shanghai, China
5 Department of Applied Mathematics, Hong Kong Polytechnic University, Hong Kong, China
6 School of Mathematics and Statistics, Huaiyin Normal University, Huaian, China
7 School of Public Health, Li Ka Shing Faculty of Medicine, University of Hong Kong, Hong Kong, China
8 Department of Medical Engineering and Technology, Xinjiang Medical University, Urumqi, 830011, China
9 School of Nursing, Hong Kong Polytechnic University, Hong Kong, China
* Correspondence to: zhaoshi.cmsa@gmail.com (SZ), weimingwang2003@163.com (WW), and daihai.he@polyu.edu.hk (DH)

Email address of all authors
SZ: zhaoshi.cmsa@gmail.com
PC: cphcc@smu.edu.cn
DG: dzgao@shnu.edu.cn
ZZ: larry.zhuang@polyu.edu.hk
YC: yonglicai@hytc.edu.cn
JR: jimran@connect.hku.hk
MKCC: marc@cuhk.edu.hk
KW: wangkaimath@sina.com
YL: yijun.lou@polyu.edu.hk
WW: weimingwang2003@163.com
LY: l.yang@polyu.edu.hk
DH: daihai.he@polyu.edu.hk
MHW: maggiew@cuhk.edu.hk
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Main text

To the Editor

Coronavirus disease 2019 (COVID-19), caused by the severe acute respiratory syndrome coronavirus 2 (SARS-CoV-2), emerged in Wuhan, China in the end of 2019, and soon spread oversea. A comprehensive and timely review summarized the scientific research in estimating the basic reproduction number ($R_0$) released from 1 January to 7 February 2020 [1]. During the early outbreak, when the key epidemiological features of COVID-19 were uncovered, the $R_0$ estimation largely relied on the growth rate of the epidemic curve and the estimation of the serial interval (SI). Here, we demonstrated that an overlarge SI would lead to overestimation of $R_0$.

We adopted the growing process proposed in [2] deterministically with a population of 11 million in Wuhan, 1 case initially onset on 5 December 2019 and a fixed step at 1 day. We consider two values of the mean serial interval (SI) that are

- SI at 4.6 days estimated based on 28 records of transmission chains [3], which was largely consistent with the SI estimate at 4.4 days based on 71 records [4]; and
- SI at 8 days, which was closer to the SI of the severe acute respiratory syndrome (SARS, 8.4 days), SI of the Middle East respiratory syndrome (MERS, 7.6 days).

As for demonstration that a larger SI could lead to overestimation in $R_0$, we conducted the simulation with two schemes that are

- Scheme (I): $R_0 = 2$, and SI = 4.6 days; and
- Scheme (II): $R_0 = 2, 3, 4$ and $3.3$ as summarized in [1], and SI = 8 days.

We also compared the simulation results with the previous estimates of the cumulative number of COVID-19 infection in Wuhan. In Fig 1, the simulation results of the scheme (I) had almost the same growing trends as those of scheme (II) with $R_0 = 3.3$. Although a higher $R_0$ could force the epidemic curve increasing rapidly, a shorter SI could increase iteration of transmission generation, i.e., transmission may occur shortly post infection.

According to the simple approximated formula that $R_0 = \exp(\gamma \cdot \text{SI})$, where $\gamma$ was the exponential growth rate calculated from the incidence data directly, a longer SI would lead to a higher $R_0$ estimate theoretically. With a shorter SI at 4.6 days, which was supported by richer datasets in [3, 4], the $R_0$ of COVID-19 could be lower than previous estimates based on longer SI. By using the growth rate ($\gamma$) at 0.15 per day, the $R_0$ was found at 2.0 with SI at 4.6 days, whereas 3.3 with SI at 8 days. Although the effects of public health control were ignored in this analysis, our model could be
extended by introducing an effective reproduction number accounting for the effectiveness of the control measures, and we remarked this modification would not affect the main conclusion. Furthermore, as pointed out in [3], provided that the SI of COVID-19 might be shorter than its incubation period, pre-symptomatic transmission may occur shortly after being infected [5]. This implies that a fraction of transmissions cannot be prevented solely through isolating the symptomatic cases, since the time when contact tracing is conducted, they may have already been infectious and generated secondary cases. Therefore, the effectively quarantine of suspected (and probable) cases, as well as close contacts, and timely contact tracing were crucial in successful outbreak mitigation.
Declarations

**Ethics approval and consent to participate**

Since no real-world data was used in this work, neither ethical approval nor individual consent was not applicable.

**Availability of materials**

There was no real-world data used in this work, the estimates from previous studies can be found in the supplementary material S1, and the key R code was attached in supplementary material S2.

**Consent for publication**

Not applicable.

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**Conflict of Interests**

DH declares receiving funding from Alibaba (China)-Hong Kong Polytechnic University Collaborative Research project. Other authors declare no competing interests.

**Authors’ Contributions**

SZ and DH conceived the study, carried out the analysis, and drafted the first manuscript. All authors discussed the results, critically read and revised the manuscript, and gave final approval for publication.
References


The simulated (curves) and previously estimated (dots) cumulative number of COVID-19 cases in Wuhan, China. The bold (main results) and dashed (alternative scenarios) curves are the simulation results. The curves in green are the simulation with SI at 8 days. The curve in black is the simulation with SI at 4.6 days. The triangular dots are the previously estimates of the COVID-19 infections, and the details can be found in the Supplementary Material S1.